



# Synthesis of $(1-x)\text{ZnAl}_2\text{O}_4-x\text{TiO}_2$ microwave dielectric ceramics by molten-salt process

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## ABSTRACT

Sintering characteristic, phase compositions, microstructures and microwave dielectric properties of  $(1-x)\text{ZnAl}_2\text{O}_4-x\text{TiO}_2$  ceramics synthesized by LiCl and  $\text{ZnCl}_2$  molten-salt were investigated. Molten-salt process can prepare smaller and more homogenous grains than the solid-state reaction method, and can lower effectively its densification temperature. Besides  $\text{ZnAl}_2\text{O}_4$  spinel and rutile main phase, sometimes  $\text{Zn}_2\text{Ti}_3\text{O}_8$  phase could exist in the ceramic system, which is closely related to  $\text{TiO}_2$  content or sintering temperature. When  $x$  value is equal to 0.25, a stable-temperature  $(1-x)\text{ZnAl}_2\text{O}_4-x\text{TiO}_2$  ceramics calcined at  $900^\circ\text{C}$  in LiCl molten-salt and sintered at  $1300^\circ\text{C}$  in air can be obtained, and exhibits microwave dielectric properties with an  $\epsilon_r$  value of 9.8, a  $Q \cdot f$  value of 27,000 GHz, and a  $\tau_f$  value of  $-7.1 \text{ ppm}/^\circ\text{C}$ .  $\text{ZnCl}_2$  molten-salt can improve significantly the quality factor ( $Q \cdot f = 56,440 \text{ GHz}$ ), however, deteriorate the temperature coefficient of resonant frequency ( $\tau_f = -25.4 \text{ ppm}/^\circ\text{C}$ ) of the ceramics.

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## 1. Introduction

For application to millimeter-wave systems, microwave dielectric materials require a low dielectric constant ( $\epsilon_r$ ) to minimize the cross-coupling effect with conductors and shorten the time for the electronic signal transition, a high quality factor ( $Q \cdot f$ ) to increase their selectivity, and a near-zero temperature coefficient of resonant frequency ( $\tau_f$ ) to ensure the stability of the frequency against temperature changes [1].

In 2005, Surendran et al. [2] suggested that  $\text{ZnAl}_2\text{O}_4\text{--TiO}_2$  spinel-based ceramics have outstanding electrical insulating properties, thermochemical stability properties, thermal-expansion properties, and they can be proposed as potential microwave substrate and antenna materials substituting for the commonly used alumina substrate. Lei et al. [3–5] had studied the sintering processes and microwave dielectric properties of  $(1-x)\text{ZnAl}_2\text{O}_4-x\text{TiO}_2$  ceramics, and found that the optimal properties can be achieved in  $(1-x)\text{ZnAl}_2\text{O}_4-x\text{TiO}_2$  ( $x=0.21$ ) ceramics calcined at  $1150^\circ\text{C}$  and sintered at  $1500^\circ\text{C}$  for 3 h at a heating rate of  $5^\circ\text{C}/\text{min}$ , with  $\epsilon_r$  value of 11.6,  $Q \cdot f$  value of 74,000 GHz (at about 6.5 GHz), and  $\tau_f$  value of  $-0.4 \text{ ppm}/^\circ\text{C}$ .

However, the sintering temperature of the  $(1-x)\text{ZnAl}_2\text{O}_4-x\text{TiO}_2$  ( $x=0.21$ ) ceramics is too high and needs to be decreased.  $\text{ZnAl}_2\text{O}_4$  fine powders can be easily synthesized through

wet chemical routes such as the coprecipitated products, citric acid route, Pechini method, hydrothermal synthesis method, sol–gel method and evaporation-induced self-assembly method [6,7], and sintering temperature can be reduced significantly. Furthermore, molten-salt process is also a well established low temperature synthesis technique that has recently attracted increasing interest. It has been used to synthesize low melting electroceramic powders and high temperature complex oxide powders [8], however, are not still found for  $\text{ZnAl}_2\text{O}_4$ -based ceramics preparation. In this study, the effects of molten-salt process on sintering characteristics, phase compositions, microstructures and microwave dielectric properties of  $(1-x)\text{ZnAl}_2\text{O}_4-x\text{TiO}_2$  ceramics were investigated.

## 2. Experimental procedure

Reagent-grade  $\text{ZnO}$ ,  $\text{Al}_2\text{O}_3$ ,  $\text{TiO}_2$  (Rutile), LiCl and  $\text{ZnCl}_2$  powders were used as raw materials. The weight ratio of LiCl (or  $\text{ZnCl}_2$ ) salt to  $(1-x)\text{ZnAl}_2\text{O}_4-x\text{TiO}_2$  ( $x=0.21, 0.23$  and  $0.25$ ) powder is 3:1. The  $(1-x)\text{ZnAl}_2\text{O}_4-x\text{TiO}_2$  powder added salts were milled with agate balls in ethanol for 3 h at a speed of 360 rpm (rotations per minute). The slurry was dried at  $80^\circ\text{C}$  in an infrared stove, and then calcined in air at  $900^\circ\text{C}$  for 3 h. The molten-salts were removed from the products by washing several times with hot deionized water until the filtrate gave no reaction with silver nitrate solution. Then, after drying again, to the calcined powders, 7 wt.% polyvinyl alcohol was added, whose concentration in the aqueous solution was 5 wt.%, and a binder was uniaxially pressed into the samples with dimensions of 20 mm in diameter and about 10 mm in height under a pressure of 150 MPa. After sintered at  $1250\text{--}1425^\circ\text{C}$  for 3 h at a heating rate of  $5^\circ\text{C}/\text{min}$  in air, these samples were cooled at a rate of  $2^\circ\text{C}/\text{min}$  up to  $1000^\circ\text{C}$  and then they were furnace cooled.

The particle size was tested using laser particle size analyzer (Winner 2000). The crystalline phases were analyzed by means of the X-ray diffraction method using  $\text{Cu K}\alpha$  radiation (XRD, X'Pert PRO, PANalytical B.V., the Netherlands). The microstructure observation was performed by field scanning electron microscope (FSEM, Sirion 200, FEI, the Netherlands). The bulk density of the sintered pellets was measured

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using the Archimedes method. The permittivity ( $\epsilon_r$ ) and the unloaded  $Q$ -factor value were measured in the TE011 mode by Hakki and Coleman method [9] using an Advantest R3767C network analyzer and parallel silver boards. The temperature coefficient of resonant frequency ( $\tau_f$ ) in the temperature range of 20–80 °C was calculated by formula (1):

$$\tau_f = \frac{f_2 - f_1}{f_1(T_2 - T_1)} \quad (1)$$

where  $f_1$  and  $f_2$  represent the resonant frequencies at  $T_1$  and  $T_2$ , respectively.

### 3. Results and discussions

#### 3.1. Powder particle size

Fig. 1 illustrates particle size distributions of the raw powders and composite powders synthesized at 900 °C for 3 h in LiCl or ZnCl<sub>2</sub> salt. Only one peak at about 2 μm appears for ZnO and TiO<sub>2</sub> raw powders, while four peaks for Al<sub>2</sub>O<sub>3</sub> starting powder can be observed, as shown in Fig. 1(a). After ZnO reacting with Al<sub>2</sub>O<sub>3</sub> and TiO<sub>2</sub> powders in molten-salt, particle size distributions of composite powders are similar to that of the Al<sub>2</sub>O<sub>3</sub> starting powder (see Fig. 1(b)), which indicates that Al<sub>2</sub>O<sub>3</sub> is used as a “template” due to its solubility in the two kinds of molten-salt both greatly lower than that of ZnO and TiO<sub>2</sub> [8].

Table 1 shows average particle diameter of the raw powders and composite powders synthesized at 900 °C for 3 h in LiCl or ZnCl<sub>2</sub> salt.  $D_{av}$  value of the  $(1-x)\text{ZnAl}_2\text{O}_4-x\text{TiO}_2$  ( $x=0.21$ ) powder (18.83 μm) prepared in LiCl is lower than that of Al<sub>2</sub>O<sub>3</sub> raw powder (27.75 μm) because Al<sub>2</sub>O<sub>3</sub> particles partly solute in the molten-salt. As the  $x$

**Table 1**

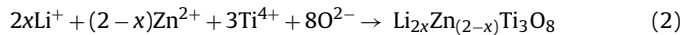
Average particle diameter ( $D_{av}$ ) of the raw powders and composite powders synthesized at 900 °C for 3 h in LiCl or ZnCl<sub>2</sub> salt.

Powder	Molten-salt	$D_{av}$ (μm)
ZnO	–	2.40
Al <sub>2</sub> O <sub>3</sub>	–	27.75
TiO <sub>2</sub>	–	1.94
0.79ZnAl <sub>2</sub> O <sub>4</sub> –0.21TiO <sub>2</sub>	LiCl	18.83
0.75ZnAl <sub>2</sub> O <sub>4</sub> –0.25TiO <sub>2</sub>	LiCl	27.75
0.75ZnAl <sub>2</sub> O <sub>4</sub> –0.25TiO <sub>2</sub>	ZnCl <sub>2</sub>	15.36

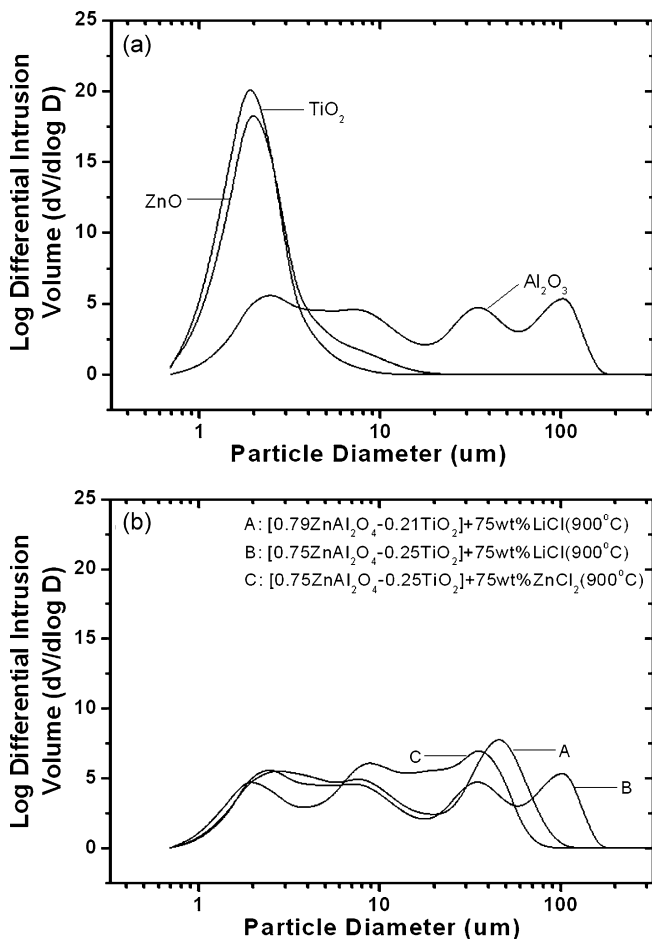
value increases to 0.25,  $(1-x)\text{ZnAl}_2\text{O}_4-x\text{TiO}_2$  particle size grows which indicates that TiO<sub>2</sub> can improve ion diffusivity and promote the particle growth. Compared with  $(1-x)\text{ZnAl}_2\text{O}_4-x\text{TiO}_2$  ( $x=0.25$ ) powder in LiCl molten-salt, the powder in ZnCl<sub>2</sub> molten-salt has smaller  $D_{av}$  value (15.36 μm), possibly because Al<sub>2</sub>O<sub>3</sub> powder has higher solubility in the latter.

#### 3.2. XRD analysis

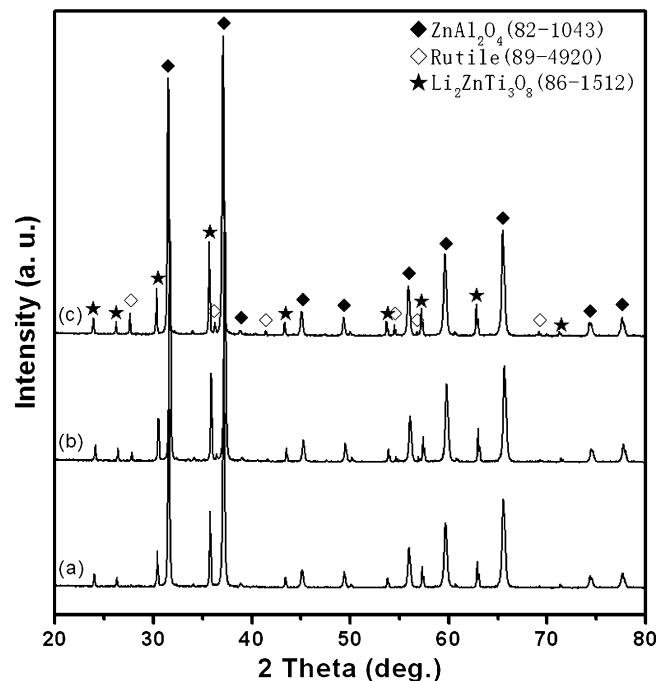
XRD patterns of  $(1-x)\text{ZnAl}_2\text{O}_4-x\text{TiO}_2$  powders synthesized at 900 °C for 3 h in LiCl salt are shown in Fig. 2. ZnAl<sub>2</sub>O<sub>4</sub> spinel and Li<sub>2x</sub>Zn<sub>(1-x)</sub>Ti<sub>3</sub>O<sub>8</sub> phases are included in the  $(1-x)\text{ZnAl}_2\text{O}_4-x\text{TiO}_2$  ( $x=0.21$ ) powder (see Fig. 2(a)). When  $x$  value reaches over 0.23, a new rutile phase appears in the  $(1-x)\text{ZnAl}_2\text{O}_4-x\text{TiO}_2$  system (see Fig. 2(b) and (c)). Moreover, X-ray intensity of the Li<sub>2x</sub>Zn<sub>(2-x)</sub>Ti<sub>3</sub>O<sub>8</sub> and rutile phase enhances gradually with the increase of TiO<sub>2</sub> content, as shown in Fig. 2. Formation of Li<sub>2x</sub>Zn<sub>(2-x)</sub>Ti<sub>3</sub>O<sub>8</sub> phase can be expressed as follows:



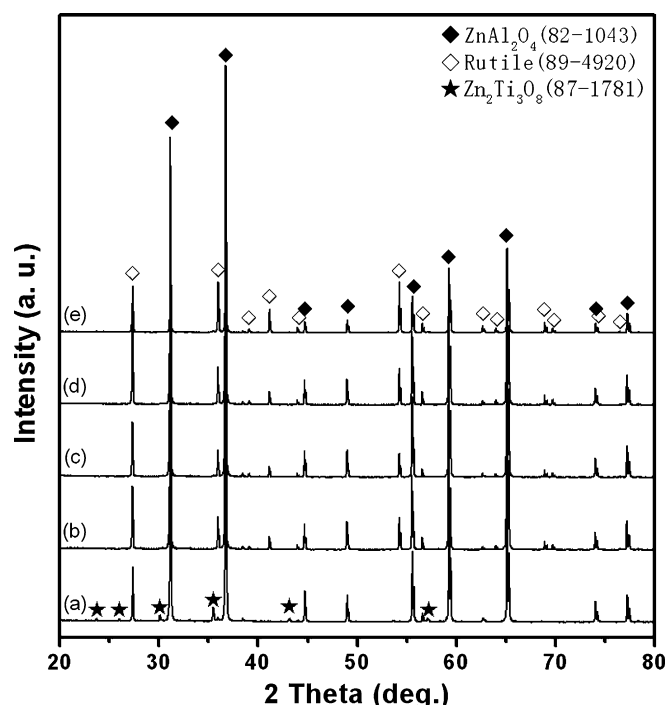
It is known from formula (2) that an increase in Ti<sup>4+</sup> ions are helpful to form Li<sub>2x</sub>Zn<sub>(2-x)</sub>Ti<sub>3</sub>O<sub>8</sub> phase, at the same time, Li<sup>+</sup> and Zn<sup>2+</sup> ions are also required. In LiCl molten-salt, Li<sup>+</sup> ions are enough, however, Zn<sup>2+</sup> ions added are limited. Therefore, as the amount of TiO<sub>2</sub> increases, Li<sub>2x</sub>Zn<sub>(2-x)</sub>Ti<sub>3</sub>O<sub>8</sub> phase increases gradually. When Zn<sup>2+</sup> ions run out, Li<sup>+</sup> ions could not form a kind of stable reac-



**Fig. 1.** Particle size distributions of (a) the raw powders and (b) composite powders synthesized at 900 °C for 3 h in LiCl or ZnCl<sub>2</sub> salts.



**Fig. 2.** XRD patterns of  $(1-x)\text{ZnAl}_2\text{O}_4-x\text{TiO}_2$  powders synthesized at 900 °C for 3 h in LiCl salt: (a)  $x=0.21$ ; (b)  $x=0.23$ ; (c)  $x=0.25$ .



**Fig. 3.** XRD patterns of  $(1-x)\text{ZnAl}_2\text{O}_4-x\text{TiO}_2$  ceramics calcined at  $900^\circ\text{C}$  for 3 h in LiCl salt and sintered at different temperatures for 3 h: (a)  $x=0.21$ ,  $1425^\circ\text{C}$ ; (b)  $x=0.23$ ,  $1300^\circ\text{C}$ ; (c)  $x=0.25$ ,  $1250^\circ\text{C}$ ; (d)  $x=0.25$ ,  $1300^\circ\text{C}$ ; (e)  $x=0.25$ ,  $1400^\circ\text{C}$ .

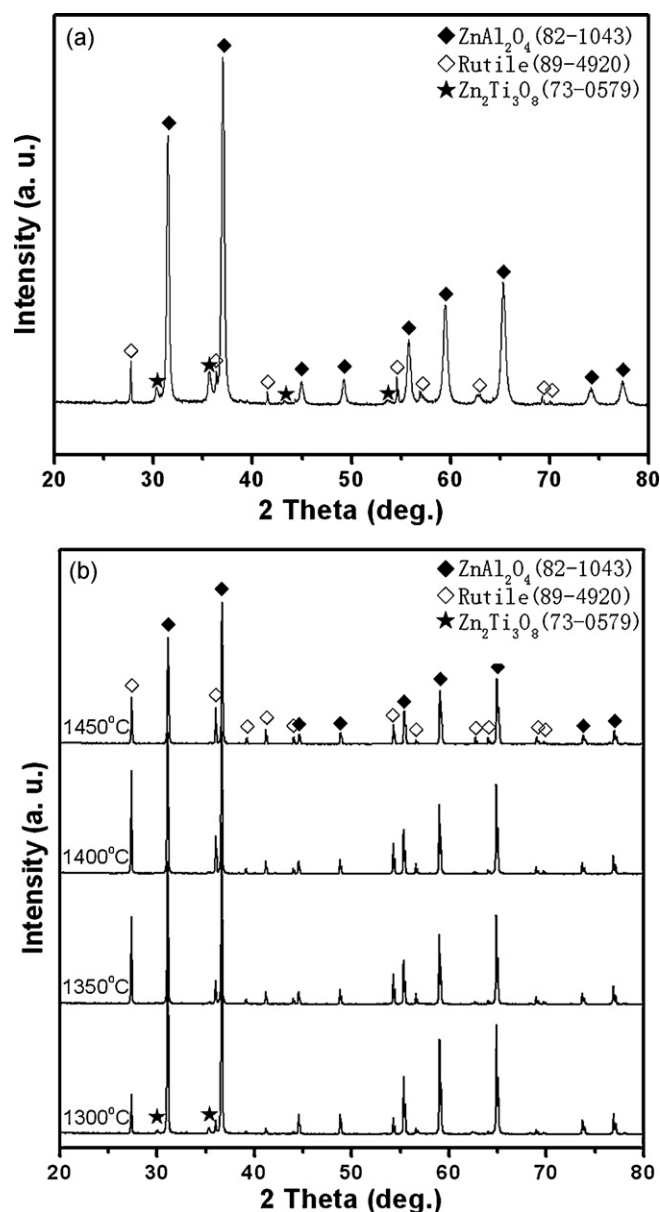
tant with  $\text{Ti}^{4+}$  ions during the cooling process, and redundant  $\text{Ti}^{4+}$  ions exist finally as rutile phase. The X-ray intensity of any phase is proportional to the relative volume fraction of the phase [3], therefore, an increase in  $\text{TiO}_2$  content results in enhancement in X-ray intensity of the  $\text{Li}_{2x}\text{Zn}_{(2-x)}\text{Ti}_3\text{O}_8$  and rutile phase, as shown in Fig. 2.

Fig. 3 shows XRD patterns of  $(1-x)\text{ZnAl}_2\text{O}_4-x\text{TiO}_2$  ceramics calcined at  $900^\circ\text{C}$  for 3 h in LiCl salt and sintered at different temperatures for 3 h. It seems that phase composition in the  $(1-x)\text{ZnAl}_2\text{O}_4-x\text{TiO}_2$  system is only relative to  $\text{TiO}_2$  content and independent of sintering temperature, as shown in Fig. 3. When  $x$  value is equal to 0.21,  $\text{ZnAl}_2\text{O}_4$  spinel, rutile and  $\text{Zn}_2\text{Ti}_3\text{O}_8$  phases ( $\text{Li}^+$  ions in  $\text{Li}_{2x}\text{Zn}_{(2-x)}\text{Ti}_3\text{O}_8$  phase vaporize easily over  $1000^\circ\text{C}$  [10]) can be observed in the ceramics, while  $\text{Zn}_2\text{Ti}_3\text{O}_8$  phase disappears for  $x \geq 0.23$ , because  $\text{TiO}_2$  can improve ion diffusion and promote  $\text{Zn}^{2+}$  ion reaction with  $\text{Al}^{3+}$  ion to form  $\text{ZnAl}_2\text{O}_4$ . As the sintering temperature increases, the X-ray intensity of rutile phase in the  $(1-x)\text{ZnAl}_2\text{O}_4-x\text{TiO}_2$  ( $x=0.25$ ) ceramics enhances gradually and that of  $\text{ZnAl}_2\text{O}_4$  spinel phase weakens progressively, as shown in Fig. 3(c)–(e), because the  $\text{TiO}_2$  grains grow easily with the increasing of the sintering temperature [3].

Fig. 4 represents the XRD patterns of  $(1-x)\text{ZnAl}_2\text{O}_4-x\text{TiO}_2$  ( $x=0.25$ ) powder synthesized at  $900^\circ\text{C}$  for 3 h in  $\text{ZnCl}_2$  salt and ceramics sintered at different temperatures for 3 h. It can be observed that  $\text{ZnAl}_2\text{O}_4$  spinel, rutile and  $\text{Zn}_2\text{Ti}_3\text{O}_8$  phases exist in the  $(1-x)\text{ZnAl}_2\text{O}_4-x\text{TiO}_2$  ( $x=0.25$ ) powder, as shown in Fig. 4(a). When the sintering temperature is  $1300^\circ\text{C}$ , the phase composition in the ceramics is the same as that in the powder, and  $\text{Zn}_2\text{Ti}_3\text{O}_8$  phase disappears until  $1450^\circ\text{C}$ , as shown in Fig. 4(b).

### 3.3. Microstructures

Fig. 5 shows scanning electron micrographs of  $(1-x)\text{ZnAl}_2\text{O}_4-x\text{TiO}_2$  ceramics prepared by the solid-state reaction and molten-salt process. Compared with the microstructure of  $(1-x)\text{ZnAl}_2\text{O}_4-x\text{TiO}_2$  ( $x=0.21$ ) ceramics synthesized by

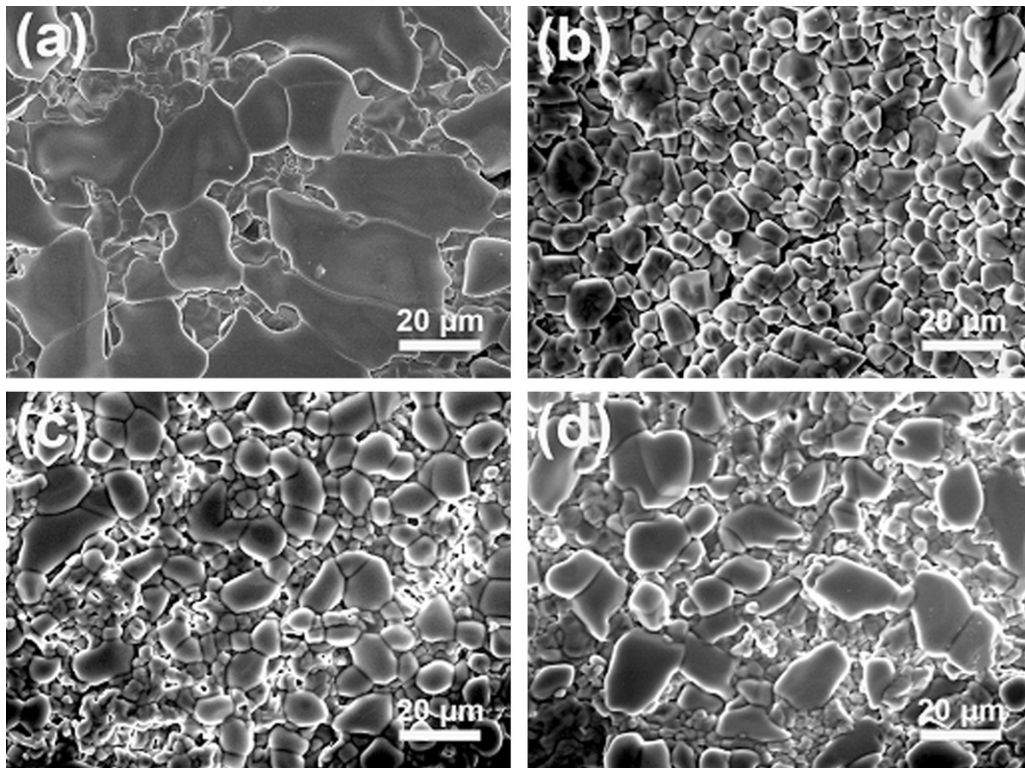


**Fig. 4.** XRD patterns of  $(1-x)\text{ZnAl}_2\text{O}_4-x\text{TiO}_2$  ( $x=0.25$ ) (a) powder synthesized at  $900^\circ\text{C}$  for 3 h in  $\text{ZnCl}_2$  salt and (b) ceramics sintered at different temperatures for 3 h.

the solid-state reaction with the bigger rutile grains ( $>50\ \mu\text{m}$ ) and the smaller  $\text{ZnAl}_2\text{O}_4$  grains (about  $5\ \mu\text{m}$ ) [5] (see Fig. 5(a)), that of the ceramics prepared by LiCl molten-salt exhibits some smaller and more homogenous grains (see Fig. 5(b)). When  $x$  value reaches 0.25, the rutile grains grow quickly (see Fig. 5(c)). Moreover, the average size of larger rutile grains in the  $(1-x)\text{ZnAl}_2\text{O}_4-x\text{TiO}_2$  ( $x=0.25$ ) ceramics synthesized by  $\text{ZnCl}_2$  molten-salt increases further (see Fig. 5(d)), compared with that in Fig. 5(c).

### 3.4. Microwave dielectric properties

Density and microwave dielectric properties of  $(1-x)\text{ZnAl}_2\text{O}_4-x\text{TiO}_2$  ceramics are shown in Table 2. LiCl and  $\text{ZnCl}_2$  molten-salt process can lower the densification temperature of  $(1-x)\text{ZnAl}_2\text{O}_4-x\text{TiO}_2$  ceramics. In comparison to  $(1-x)\text{ZnAl}_2\text{O}_4-x\text{TiO}_2$  ( $x=0.21$ ) ceramics prepared by the solid-state reaction (No. 1), the ceramics synthesized by LiCl molten-salt process (No. 2) has lower bulk density,  $\epsilon_r$  and  $Q \cdot f$  value, and more negative  $\tau_f$  value. On one hand,  $\text{Li}^+$  ions vaporize easily



**Fig. 5.** Scanning electron micrographs of  $(1-x)\text{ZnAl}_2\text{O}_4-x\text{TiO}_2$  ceramics: (a)  $x=0.21$ , solid-state reaction,  $1500^\circ\text{C}$ ; (b)  $x=0.21$ , LiCl salt,  $1425^\circ\text{C}$ ; (c)  $x=0.25$ , LiCl salt,  $1300^\circ\text{C}$ ; (d)  $x=0.25$ ,  $\text{ZnCl}_2$  salt,  $1350^\circ\text{C}$ .

**Table 2**

Density and microwave dielectric properties of  $(1-x)\text{ZnAl}_2\text{O}_4-x\text{TiO}_2$  ceramics.

No.	$x$	Molten-salt	$T_{\text{cal}} (^\circ\text{C})$	$T_{\text{sint}}^a (^\circ\text{C})$	$\varepsilon_r$	$Qf$ (GHz)	$\tau_f$ (ppm/ $^\circ\text{C}$ )	$\rho$ (g/cm $^3$ )
1	0.21	–	1150	1500	11.6	74,000	–0.4	4.42
2	0.21	LiCl	900	1425	10.0	39,970	–19.7	4.13
3	0.25	LiCl	900	1300	9.8	27,000	–7.1	4.15
4	0.25	$\text{ZnCl}_2$	900	1350	10.0	56,440	–25.4	4.39

<sup>a</sup>  $T_{\text{sint}}$  is densification temperature.

over  $1000^\circ\text{C}$  to form micropores, on the other hand, as the grain size reduces, the number of triangular grain boundary increases, therefore micropores increase and bulk density decreases. At the same time, an increase in micropores leads to reduction in  $\varepsilon_r$  and  $Qf$  values. Moreover, the amount of  $\text{TiO}_2$  phase with highly positive  $\tau_f$  value in the  $(1-x)\text{ZnAl}_2\text{O}_4-x\text{TiO}_2$  ( $x=0.21$ ) system synthesized by LiCl molten-salt process reduces due to formation of  $\text{Zn}_2\text{Ti}_3\text{O}_8$  second phase, which results in more negative  $\tau_f$  value on the basis of the mixing rule [3]. When  $x$  value increases from 0.21 to 0.25,  $\text{Zn}_2\text{Ti}_3\text{O}_8$  second phase disappears (see Fig. 3(a)) and the amount of  $\text{TiO}_2$  phase in the system increases, therefore, the  $\tau_f$  value can be adjusted to near zero ( $-7.1$  ppm/ $^\circ\text{C}$ ) and densification temperature can be lowered from  $1425$  to  $1300^\circ\text{C}$ . Although  $\text{TiO}_2$  content in No. 3 is more than that in No. 1, the  $\tau_f$  value of the former is slightly lower than that of the latter, which indicates that  $\text{Ti}^{4+}$  ions in the system prepared by LiCl molten-salt process could diffuse more easily into the crystal lattice of the  $\text{ZnAl}_2\text{O}_4$  spinel phase.  $\text{Zn}_2\text{Ti}_3\text{O}_8$  has the same spinel structure as  $\text{ZnAl}_2\text{O}_4$ , however, their lattice constants have great difference, so they can only form limited solid solution. When LiCl was replaced by  $\text{ZnCl}_2$  molten-salt, the  $\tau_f$  value of the  $(1-x)\text{ZnAl}_2\text{O}_4-x\text{TiO}_2$  ( $x=0.25$ ) ceramics (No. 4) reduces to  $-25.4$  ppm/ $^\circ\text{C}$ , which could result from the effect of  $\text{Zn}_2\text{Ti}_3\text{O}_8$  phase in the system, as shown in Fig. 4(b). The  $Qf$  value of No. 4 is twice more than that of No. 3 due to the higher bulk density of the former.

#### 4. Conclusions

In the  $(1-x)\text{ZnAl}_2\text{O}_4-x\text{TiO}_2$  system, LiCl and  $\text{ZnCl}_2$  molten-salt process can prepare smaller and more homogenous grains than the solid-state reaction method, and can effectively lower its densification temperature.  $\text{Li}_{2x}\text{Zn}_{(2-x)}\text{Ti}_3\text{O}_8$  (or  $\text{Zn}_2\text{Ti}_3\text{O}_8$ ) low temperature phase exists easily in the calcined powder synthesized by molten-salt, and it reduces gradually until disappears with the increase of  $\text{TiO}_2$  content or sintering temperature. In general, the  $\varepsilon_r$  value of the  $(1-x)\text{ZnAl}_2\text{O}_4-x\text{TiO}_2$  ceramics synthesized by molten-salt process reduces slightly, and the density,  $Qf$  and  $\tau_f$  values deteriorate, however, they are closely related to the kind of molten-salt.

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